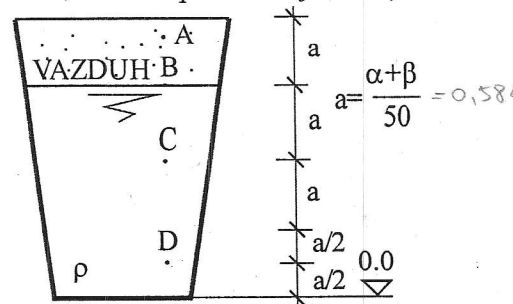


JEDNOSTAVNI ZADACI

ZADATAK 1.1

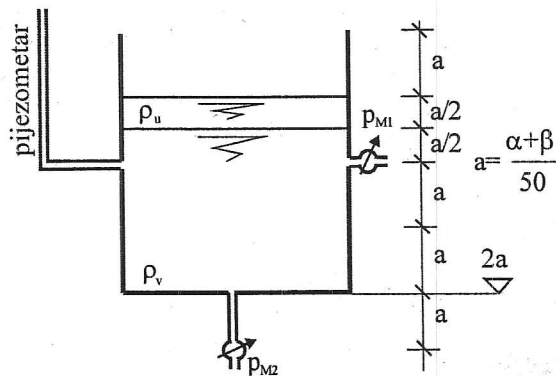
(Napomena: slike kotirati u metrima, a ne u opštim brojevima)

Rezervoar kao na slici je napunjen tečnošću gustine $\rho = 4a/3 \text{ kg/dm}^3$. Iznad površine fluida nalazi se vazduh pod pritiskom od $p_{\text{vaz}} = -\beta/2 \text{ kPa}$. Izračunati pijezirometarsku kotu fluida i hidrostatičke i apsolutne pritiske u naznačenim tačkama A, B, C i D. Gustina vazduha se zanemaruje.



ZADATAK 1.2

U rezervoaru prikazanom na slici se nalazi ulje gustine $\rho_u = 0.8 \text{ kg/dm}^3$ i voda gustine $\rho_v = 1.0 \text{ kg/dm}^3$. Izračunati pijezirometarske kote fluida, naznačiti nivo u pijezirometru i izračunati pritiske koje pokazuju manometri.

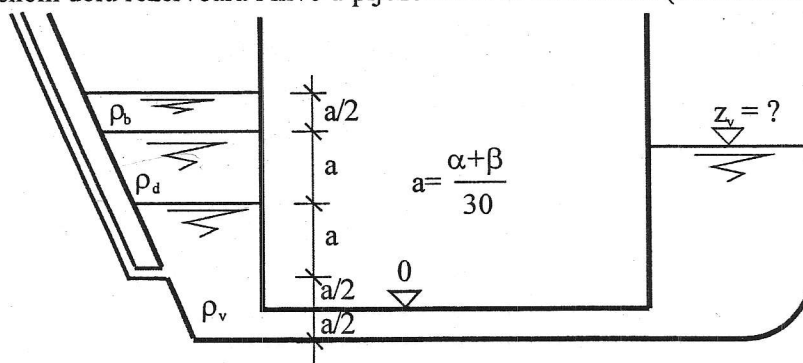


SLOŽENI ZADACI

ZADATAK 1.3

U rezervoaru kao na slici se nalaze tri fluida: benzin (gustine $\rho_b = 0.74 \text{ kg/dm}^3$), dizel ($\rho_d = 0.83 \text{ kg/dm}^3$) i voda ($\rho_v = 1.0 \text{ kg/dm}^3$). Izračunati:

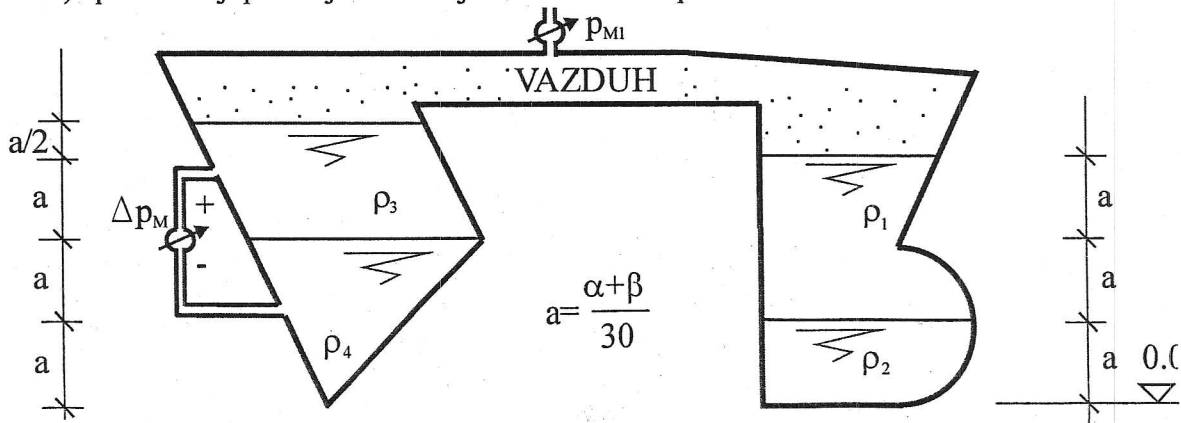
- Pijezirometarske kote fluida,
- Nivo vode u desnom delu rezervoara i nivo u pijezirometru sa leve strane (naznačiti na pijezirometru nivo)



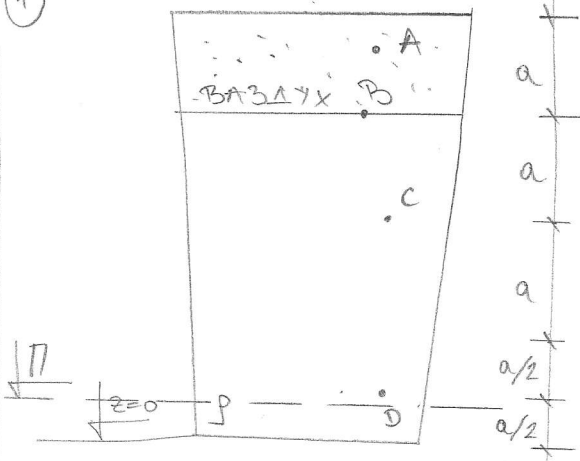
ZADATAK 1.4

U instalaciji kao na slici, nalaze se četiri fluida i vazduh pod pritiskom. Gustine fluida su $\rho_1 = 1 - \beta/200 \text{ kg/dm}^3$, $\rho_2 = 1.2 \text{ kg/dm}^3$, $\rho_3 = 1 - \beta/300 \text{ kg/dm}^3$ i $\rho_4 = \rho_2$ dok se gustina vazduha zanemaruje. Ako manometar M1 pokazuje, $p_{M1} = 0.5 \text{ bara}$, izračunati:

- Pijezirometarske kote fluida,
- pritisak koji pokazuje diferencijalni manometar Δp_M .



①



$\alpha = 5 \quad \beta = 24.2 \quad \Pi = ?$
 $a = \frac{\alpha + \beta}{50} = 0,584 \text{ m} \quad P_{\text{aps}}, P = ?$

$\rho = \frac{4a}{3} = 0,779 \text{ kg/dm}^3$
 $P_{\text{vaz}} = -\frac{\beta}{2} = -12,1 \text{ kPa}$

$\frac{P}{\rho g} + z = \Pi$

$\Pi = \frac{P_{\text{vaz}}}{\rho g} + z_B = \frac{-12,1 \cdot 10^3 \text{ Pa}}{9,81 \frac{\text{m}}{\text{s}^2} \cdot 0,779 \cdot 10^3 \frac{\text{kg}}{\text{m}^3}} + 3 \cdot 0,584 \Rightarrow \Pi = 0,169 \text{ m}$

$P_A = P_{\text{vaz}} = P_B = -12,1 \text{ kPa} \quad P_{\text{aps}(A,B)} = P + P_{\text{atm}} = -12,1 + 100 \Rightarrow P_{\text{aps}(A,B)} = 87,9 \text{ kPa}$

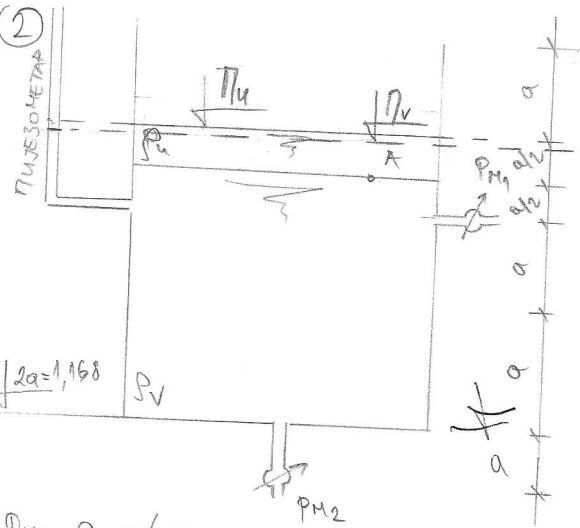
$P_C = \rho g (\Pi - z_C) = 0,779 \cdot 10^3 \frac{\text{kg}}{\text{m}^3} \cdot 9,81 \frac{\text{m}}{\text{s}^2} \cdot (0,169 \text{ m} - 2 \cdot 0,584)$

$P_C = -7,634 \text{ kPa} \quad P_{\text{aps}(C)} = -7,634 + 100 \Rightarrow P_{\text{aps}(C)} = 92,37 \text{ kPa}$

$P_D = \rho g (\Pi - z_D) = 0,779 \cdot 10^3 \frac{\text{kg}}{\text{m}^3} \cdot 9,81 \frac{\text{m}}{\text{s}^2} \cdot (0,169 \text{ m} - 0,584/2)$

$P_D = -0,939 \text{ kPa} \quad P_{\text{aps}(D)} = 100 - 0,939 \Rightarrow P_{\text{aps}(D)} = 99,06 \text{ kPa}$

②



$\rho_u = 0,8 \text{ kg/dm}^3 \quad \Pi_u = ? \quad P_{M1} = ?$
 $\rho_v = 1,0 \text{ kg/dm}^3 \quad \Pi_v = ? \quad P_{M2} = ?$

$\Pi_u = 2,92 \text{ m}$

$\frac{P_A}{\rho_u g} + z_A = \Pi_u \Rightarrow P_A = \rho_u g (\Pi_u - z_A)$

$P_A = 0,8 \cdot 10^3 \cdot 9,81 (2,92 - 2,628)$

$P_A = 2,29 \text{ kPa}$

$\Pi_v = \frac{P_A}{\rho_v g} + z_A = \frac{2,29 \cdot 10^3}{1000 \cdot 9,81} + 2,628$

$\Pi_v = 2,861 \text{ m}$

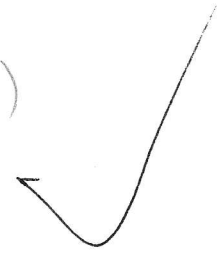
$P_{M2} = \rho_v g (\Pi_v - z_{M2})$

$P_{M2} = 1000 \cdot 9,81 (2,861 + 0,584)$

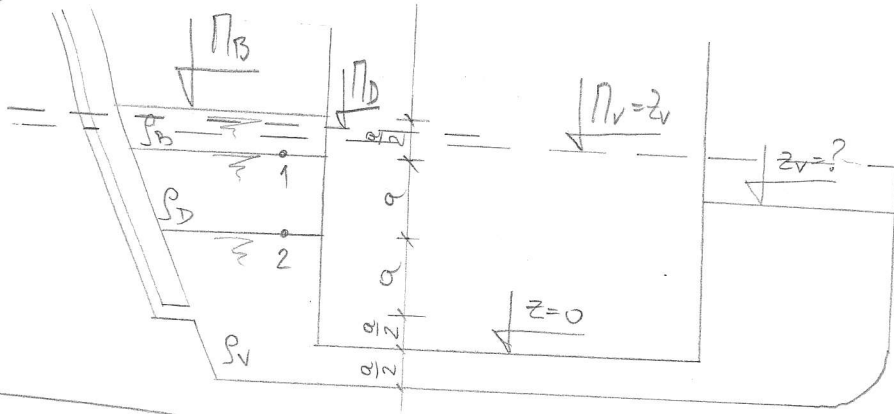
$P_{M2} = 22,34 \text{ kPa}$

$P_{M1} = 1000 \cdot 9,81 (2,861 - 2,336)$

$P_{M1} = 5,15 \text{ kPa}$



1.3



$\rho_B = 0,74 \text{ kg/dm}^3$
 $\rho_D = 0,83 \text{ kg/dm}^3$
 $\rho_V = 1,0 \text{ kg/dm}^3$
 $\Pi_B, \Pi_D, \Pi_V = ?$
 $z_V = ? \quad \alpha = 5 \quad \beta = 24,2$
 $a = \frac{\alpha + \beta}{30} = 0,973 \text{ m}$

$\Pi_B = 2,92 \text{ m}$

$P_1 = \rho_B g (\Pi_B - z_1)$

$P_1 = 0,74 \cdot 10^3 \cdot 9,81 (2,92 - 2,432)$

$P_1 = 3,54 \text{ kPa}$

$P_2 = \rho_D g (\Pi_D - z_2)$

$P_2 = 830 \cdot 9,81 (2,867 - 1,459)$

$P_2 = 11,46 \text{ kPa}$

$\Pi_D = \frac{P_1}{\rho_B g} + z_1$

$\Pi_D = \frac{3,54 \text{ kPa}}{0,74 \cdot 10^3 \cdot 9,81} + 2,432 = 2,867 \text{ m}$

$\Pi_D = 2,867 \text{ m}$

$\Pi_V = \frac{P_2}{\rho_V g} + z_2$

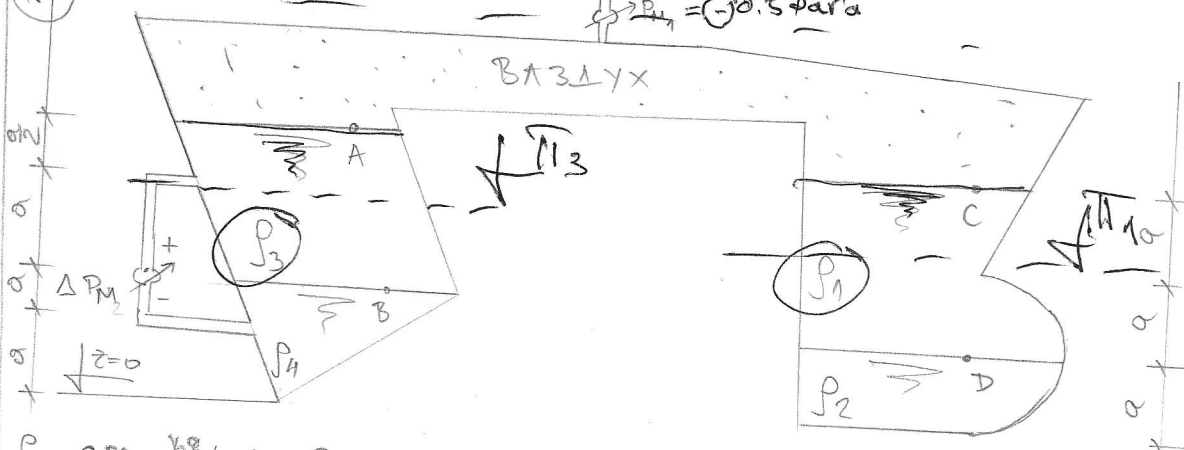
$\Pi_V = \frac{11,46 \cdot 10^3}{1000 \cdot 9,81} + 1,459 = 2,627 \text{ m}$

$\Pi_V = 2,627 \text{ m}$

$z_V = \Pi_V = 2,627 \text{ m}$

$z_V = 2,627 \text{ m}$

1.4



$\rho_1 = 0,879 \text{ kg/dm}^3$
 $\rho_2 = 1,2 \text{ kg/dm}^3$
 $\rho_3 = 0,919 \text{ kg/dm}^3$
 $\rho_4 = 1,2 \text{ kg/dm}^3$
 $P_M = 0,5 \text{ kPa} = 50 \text{ kPa}$
 $a = 0,973 \text{ m}$
 $\Pi_1, \Pi_2, \Pi_3, \Pi_4 = ?$
 $\Delta P_M = ?$

$\Pi_3 = \frac{P_M}{\rho_3 g} + z_A = \frac{50 \cdot 10^3}{0,919 \cdot 10^3 \cdot 9,81} + 3,31 = 8,959 \text{ m}$
 $\Pi_1 = \frac{P_M}{\rho_1 g} + z_C = \frac{50 \cdot 10^3}{0,879 \cdot 9,81} + 2,919 = 8,717 \text{ m}$

$\Pi_3 = 8,959 \text{ m}$

$\Pi_1 = 8,717 \text{ m}$

$P_B = \rho_3 g (\Pi_3 - z_B) = 0,919 \cdot 10^3 \cdot 9,81 (8,959 - 1,946)$

$P_B = 63,45 \text{ kPa}$

$P_D = \rho_1 g (\Pi_1 - z_D) = 0,879 \cdot 10^3 \cdot 9,81 (8,717 - 0,973)$

$P_D = 66,77 \text{ kPa}$

$\Pi_4 = \frac{P_B}{\rho_4 g} + z_B = \frac{63,45 \cdot 10^3}{1,2 \cdot 10^3 \cdot 9,81} + 1,946 = 7,310 \text{ m}$

$\Pi_4 = 7,310 \text{ m}$

$\Pi_2 = \frac{P_D}{\rho_2 g} + 0,973 = \frac{66,77 \cdot 10^3}{1,2 \cdot 10^3 \cdot 9,81} + 0,973 = 6,645 \text{ m}$

$\Pi_2 = 6,645 \text{ m}$

$\Delta P_M = 7,80 \text{ Pa}$